

Applying QRPAdef

The “classical” approach

Work mainly by J. Terasaki

Reminders

Basic Procedure

- ▶ Do deformed HFB calculation in cylindrical box.
- ▶ Construct as basis (as large as possible) of two-proton-canonical-quasiparticle and two-neutron-canonical-quasiparticle states.
- ▶ Construct energy matrix between basis states — **many 2-d integrals (with splines)** — and diagonalize.

High-Performance Computing

- ▶ Task: Typically compute about 10^{10} matrix elements in each K^π and nucleus (using about 10^5 core-hours at desired level of accuracy for heavy nuclei).
- ▶ Info/Issues:
 - ▶ Code scales well up to 10,000 cores and beyond.
 - ▶ ADLB might help with larger numbers of cores

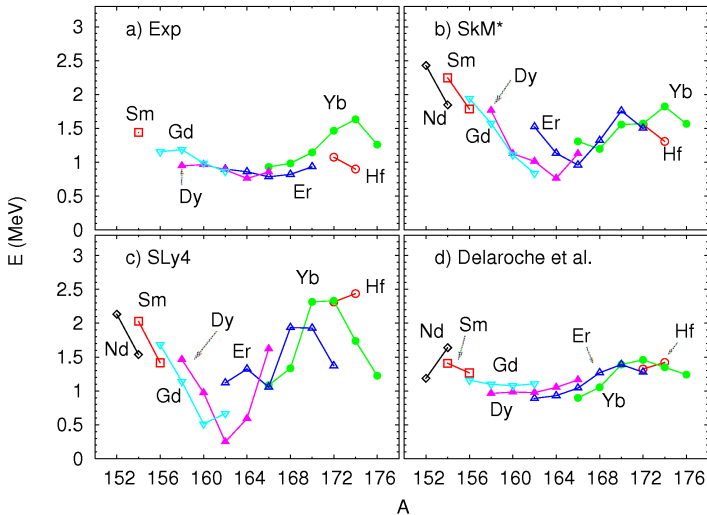
Beta and Gamma Vibrations in Rare Earths

With 10M core-hours:

Z\N	92	94	96	98	100	102	104	106	108	110
74										
72					¹⁷² Hf	¹⁷⁴ Hf				
70			¹⁶⁶ Yb	¹⁶⁸ Yb	¹⁷⁰ Yb	¹⁷² Yb	¹⁷⁴ Yb	¹⁷⁶ Yb		
68		¹⁶² Er	¹⁶⁴ Er	¹⁶⁶ Er	¹⁶⁸ Er	¹⁷⁰ Er	¹⁷² Er			
66	¹⁵⁸ Dy	¹⁶⁰ Dy	¹⁶² Dy	¹⁶⁴ Dy	¹⁶⁶ Dy					
64	¹⁵⁶ Gd	¹⁵⁸ Gd	¹⁶⁰ Gd	¹⁶² Gd						
62	¹⁵⁴ Sm	¹⁵⁶ Sm								
60	¹⁵² Nd	¹⁵⁴ Nd								
58										

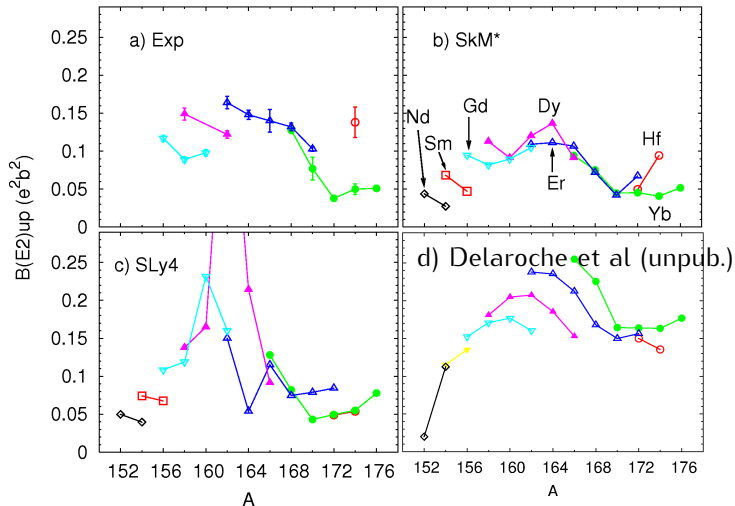
All have $\beta > 0.3$

Energies



Minimum is correct and SkM* does a very good job in Yb, but N dependence is too strong elsewhere and $SLy4 < SkM^*$.

Transition Strengths



Results seem a bit better than for energies, and Yb isotopes are good again.

Statistics

Deformed

	\bar{R}_E	σ_E	\bar{R}_Q	σ_Q
SkM*	0.28	0.18	-0.13	0.14
SLy4	0.20	0.50	-0.004	0.31

Statistics

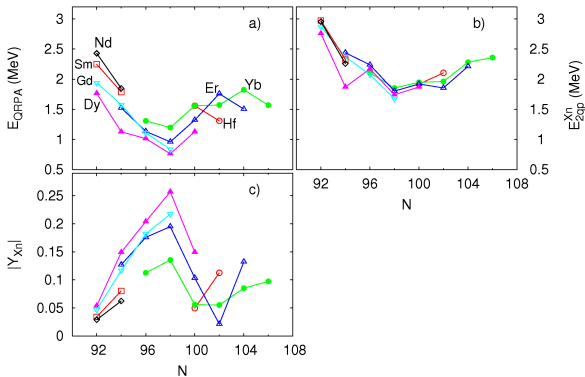
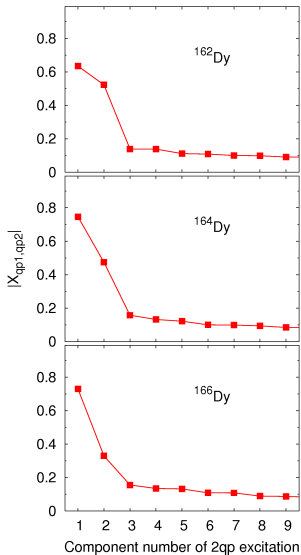
Deformed

	\bar{R}_E	σ_E	\bar{R}_Q	σ_Q
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Spherical

	\bar{R}_E	σ_E	\bar{R}_Q	σ_Q
SkM*	0.11	0.44	-0.29	0.53
SLy4	0.33	0.51	-0.32	0.42

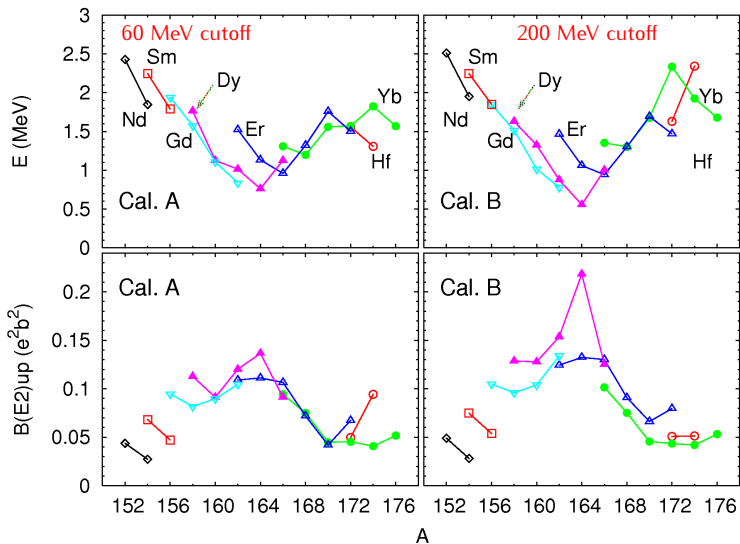
Dominance by a Few Two-qp States



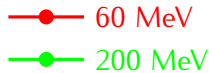
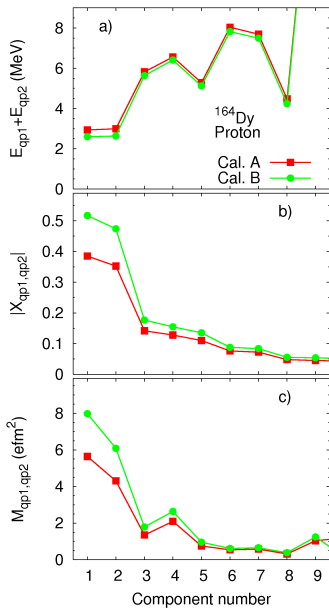
Not enough configuration mixing?

Varying Pairing Cutoff Energy

SkM*



Effects of Cutoff Variation on Two-qp Makeup



Beta Vibrations

Meh...

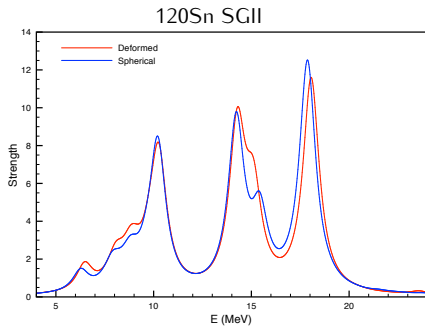
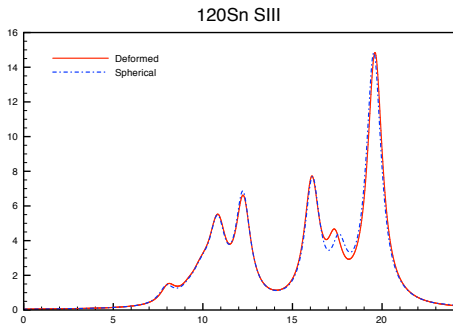
Need much larger basis — about 70,000 two-qp states. Even then, only a few nuclei have states that are uncontaminated by spurious number nonconservation.

	E_{cal}^{β} (MeV)	E_{exp}^{β} (MeV)	$B(E2)_{\text{cal}}^{\beta}$ (e^2b^2)	$B(E2)_{\text{exp}}^{\beta}$ (e^2b^2)	$S_N/S_N^{\text{spurious}}$
^{166}Yb	1.802	1.043	0.0398		0.004
^{168}Yb	2.039	1.155	0.0343		0.012
^{172}Yb	1.605	1.117	0.0049	0.0081(17)	0.054
^{170}Er	1.596	0.960	0.0030	0.0079(9)	0.054

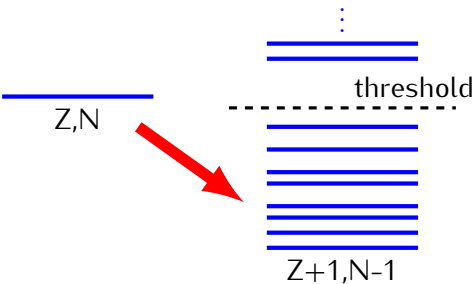
Charge-Changing Code

Two-qp basis states now contain one neutron qp and one proton qp.

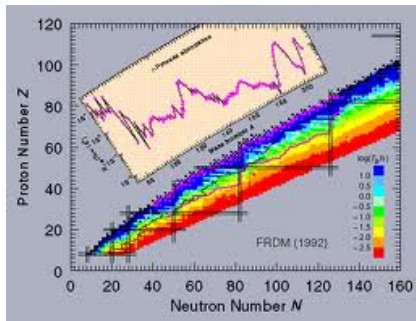
Tests



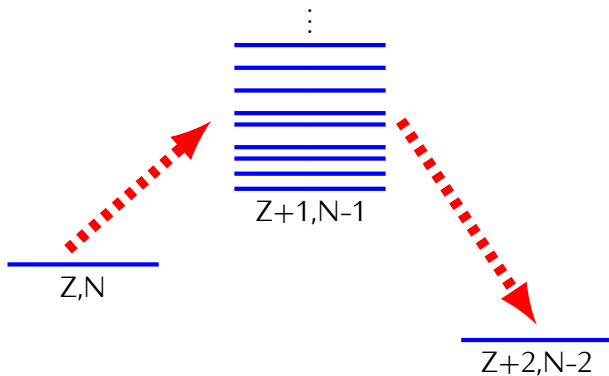
Initial Application: Light R-Process Elements



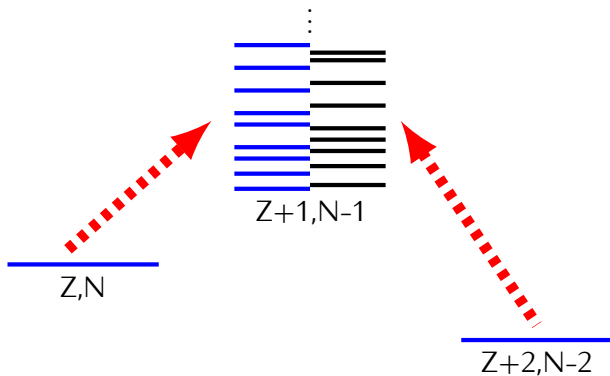
In r -process nuclei, significant fraction of GT strength is below threshold. Tom Shafer (topical-collaboration-supported student) applying first to nuclei important for formation of $A = 80$ r -process peak.



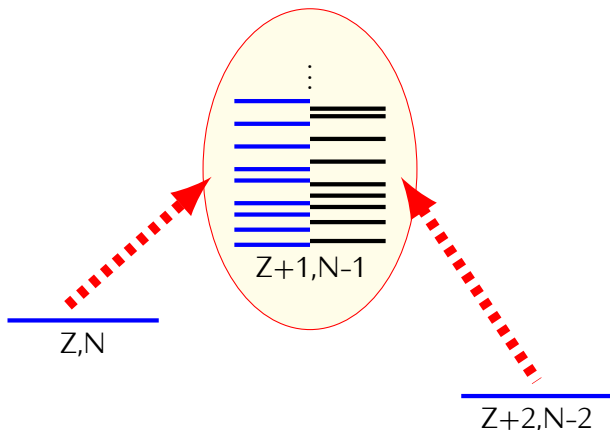
Upcoming Application: Double-Beta Decay



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Need to “debosonize” QRPA to calculate overlaps of states based on different vacua, e.g, through representation of Jancovici and Schiff. Haven’t found alternative to complicated expansion in Y ’s

Milestones, etc.

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- ▶ Finish quadrupole vibrations ✓
- ▶ Do beta decay Underway
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- ▶ Start beyond RPA Still working on this one